Data Preparation

15

by Patrick Boily, with contributions from Jen Schellinck

Once raw data has been collected and stored in a database or a dataset, the focus should shift to data cleaning and processing.

This requires testing for soundness and fixing errors, designing and implementing strategies to deal with missing values and outlying/influential observations, as well as low-level exploratory data analysis and visualization to determine what data transformations and dimension reduction approaches will be needed before embarking on a more sophisticated path.

In this chapter, we establish the essential elements of data cleaning and data processing.

15.1 Introduction

Martin K: Data is messy, Alison.

Alison M: Even after it's been cleaned?

Martin K: Especially after it's been cleaned.

(P. Boily, J. Schellinck, *The Great Balancing Act* [unpublished]).

Data cleaning and data processing are essential aspects of quantitative analysis projects; analysts and consultants should be prepared to spend up to 80% of their time on data preparation, keeping in mind that:

- processing should NEVER be done on the original dataset make copies along the way;
- ALL cleaning steps need to be documented;
- if **too much** of the data requires cleaning up, the data collection procedure might need to be **revisited**, and
- records should only be discarded as a last resort.

Another thing to keep in mind is that cleaning and processing may need to take place more than once depending on the type of data collection (one pass, batch, continuously), and that that it is essentially impossible to determine if all data issues have been found and fixed.

Note: in this chapter, we are assuming that the datasets of interest contain only numerical and/or categorical observations. Additional steps must be taken when dealing with unstructured data, such as text or images (we'll have more to say on this topic later).

15.1 Introduction	723
15.2 General Principles	724
Data Cleaning Approaches	724
Pros and Cons	724
Tools and Methods	725
15.3 Data Quality	726
Common Error Sources	727
Detecting Invalid Entries .	727
15.4 Missing Values	729
Missing Value Mechanisms	729
Imputation Methods	730
Multiple Imputation	737
15.5 Anomalous Observations .	738
Anomaly Detection	739
Outlier Tests	739
Visual Outlier Detection	742
15.6 Data Transformations	744
Common Transformations .	745
Box-Cox Transformations .	747
Scaling	751
Discretizing	751
Creating Variables	752
15.7 Example: Algae Blooms	752
Problem Description	752
Loading the Data	753
Summary & Visualization .	754
Data Cleaning	765
Principal Components	769
15.8 Exercises	771

15.2 General Principles

Dilbert: I didn't have any accurate numbers, so I just made up this one. Studies have shown that accurate numbers aren't any more useful that the ones you make up.

Pointy-Haired Boss: How many studies showed that?

Dilbert: [beat] Eighty-seven. (S. Adams, Dilbert ♂, 8 May 2008)

15.2.1 Data Cleaning Approaches

We recognize two main **philosophical** approaches to data cleaning and validation:

- methodical, and
- narrative.

The **methodical** approach consists in running through a **checklist** of potential issues and flagging those that apply to the data.

The **narrative** approach, on the other hand, consists in **exploring** the dataset while searching for unlikely or irregular patterns.

Which approach the consultant/analyst opts to follow depends on a number of factors, not the least of which is the client's needs and views on the matter – it is important to discuss this point with the clients.

15.2.2 Pros and Cons

The methodical approach focuses on **syntax**; the checklist is typically **context-independent**, which means that it (or one of its subsets) can be reused from one project to another – this makes data analysis pipelines **easy to implement** and **automate**. In the same vein, this approach allows for common errors to be **easily identified**.

On the flip side, the checklist may be quite extensive and the entire process may prove **time-consuming**, but the biggest disadvantage of the methodical approach is that it makes it difficult to identify **new types of errors**.

In contrast, the narrative approach focuses on **semantics**; even false starts may simultaneously produce **data understanding** prior to an eventual switch to a more mechanical approach.

It is easy, however, to miss important (and perhaps obvious) sources of errors as well as invalid observations when the datasets have a **large number of features**.

There is an additional downside: **domain expertise**, coupled with the narrative approach, may bias the process by neglecting "uninteresting" areas of the dataset – it takes a special person to spend time on potentially barren lands when they know that greener pastures are available just over yonder.

random missing values	values outside of expected range - in numeric		factors incorrectly/iconsiste ntly coded	date/time values in multiple formats
impossible numeric values	leading or trailing white space	badly formatted date/time values	non-random missing values	logical inconsistencies across fields
characters in numeric field	evnected range -		inconsistent or no distinction between null, 0,not available, not applicable,missing	possible factors missing
multiple symbols used for missing values	???	fields incorrectly separated in row	blank fields	logical iconsistencies within field
entire blank rows	entire blank rows character encoding issues		non-factor values in factor	numeric values in character field

Figure 15.1: Data cleaning bingo card [J. Schellinck].

15.2.3 Tools and Methods

A non-exhaustive list of common data issues can be found in the *Data Cleaning Bingo Card* (see Figure 15.1). Other methods include:

- visualizations which may help easily identify observations that need to be further examined;
- data summaries # of missing observations; 5-pt summary, mean, standard deviation, skew, kurtosis, for numerical variables; distribution tables for categorical variables;
- *n*-way tables counts for joint distributions of categorical variables;
- small multiples tables/visualizations indexed along categorical variables, and
- preliminary data analyses which may provide "huh, that's odd..."
 realizations.

It is important to note that there is nothing wrong with running a number of analyses to flush out data issues, but remember to label your initial forays as **preliminary** analyses.¹

Data scientists, dataanalysts, and quantitative consultants alike need to be comfortable with **both** approaches.

As an analogy, the narrative approach is akin to working out a crossword puzzle with a pen and accepting to put down potentially erroneous answers once in a while to try to open up the grid.²

The methodical approach, on the other hand, is similar to working out the puzzle with a pencil and a dictionary, only putting down answers when their correctness is guaranteed.³

- 1: From the client or stakeholder's perspective, repeated analyses may create a sense of unease and distrust, even if they form a crucial part of the analytical process.
- 2: What artificial intelligence researchers call the "exploration" approach.
- 3: The "exploitation" approach of artificial intelligence.

More puzzles get solved when using the first approach, but missteps tend to be spectacular. Not as many puzzles get solved the second way, but the trade-off is that it leads to fewer mistakes.

15.3 Data Quality

Calvin's Dad: OK Calvin. Let's check over your math homework.

Calvin: Let's not and say we did.

Calvin's Dad: Your teacher says you need to spend more time on it. Have a seat.

Calvin: More time?! I already spent 10 whole minutes on it! 10 minutes shot! Wasted! Down the drain!

Calvin's Dad: You've written here 8 + 4 = 7. Now you know that's not right.

Calvin: So I was off a little bit. Sue me.

Calvin's Dad: You can't **add** things and come with **less** than you started with!

Calvin: I can do that! It's a free country! I've got my rights! (B. Watterson, *Calvin and Hobbes*, 15-09-1990.)

The quality of the data has an important effect on the quality of the results: as the saying goes: "garbage in, garbage out."

Data is said to be **sound** when it has as few issues as possible with:

- validity are observations sensible, given data type, range, mandatory response, uniqueness, value, regular expressions, etc. (e.g. a value that is expected to be text value is a number, a value that is expected to be positive is negative, etc.)?;
- completeness are there missing observations (more on this in a subsequent section)?;
- accuracy and precision are there measurement and/or data entry errors (e.g., an individual has 3 children but only 2 are recorded, etc., see Figure 15.2, linking accuracy to bias and precision to the standard error)?;
- consistency are there conflicting observations (e.g., an individual has no children, but the age of one kid is recorded, etc.)?, and
- uniformity are units used uniformly throughout (e.g., an individual is 6ft tall, whereas another one is 145cm tall)?

Finding an issue with data quality after the analyses are completed is a sure-fire way of losing the stakeholder's or client's trust – check early and often!



accurate and precise



precise but not accurate



accurate but not precise



neither accurate nor very precise

Figure 15.2: Accuracy as bias, precision as standard error [author unknown].

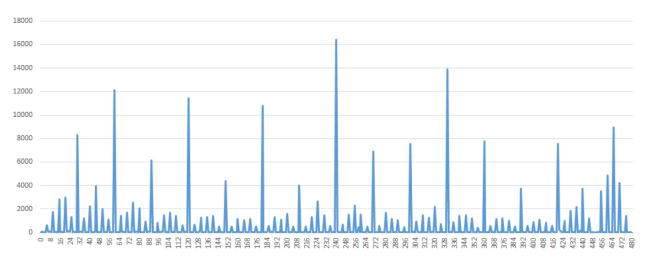


Figure 15.3: An illustration of heaping behaviour: self-reported time spent working in a day [personal file]. The entries for 7, 7.5, and 8 hours are omitted. Note the rounding off at various multiples of 5 minutes.

15.3.1 Common Error Sources

If the analysts have some control over the data collection and initial processing, regular data validation tests are easier to set-up.

When analysts are dealing with **legacy**, **inherited**, or **combined** datasets, however, it can be difficult to recognize errors that arise from:

- missing data being given a code;
- NA/blank entries being given a code;
- data entry errors;
- coding errors;
- measurement errors;
- duplicate entries;
- heaping (see Figure 15.3 for an example),
- etc.

15.3.2 Detecting Invalid Entries

Potentially invalid entries can be detected with the help of a number of methods:

- univariate descriptive statistics *z* score, count, range, mean, median, standard deviation, etc.;
- multivariate descriptive statistics *n* way tables and logic checks;
- data visualization scatterplot, histogram, joint histogram, etc. (see Chapter 16, Data Visualization and Data Exploration, and [25] for more information on the topic),
- and so on.

It is important to point out that univariate tests do not always tell the **whole** story (and may in fact obscure important details).

Example: consider, for instance, an artificial medical dataset consisting of 38 patients' records, containing, among others, fields for the **sex** and the **pregnancy status** of the patients.

A summary of the data of interest is provided in the **frequency counts** (1-way tables) of the table below:

_	Male	19	<u>+</u>	Yes	7
Sex	Female		nan	No	27
Š	(blank)	2	regn	99	1
	Total	-		(blank)	3
Total 30			Total	38	

Analysts can quickly notice that some values are missing (in green) and that an entry has been miscoded as 99 (in yellow). Using only these univariate summaries, however, it is impossible to decide what to do with these invalid entries.

The 2-way frequency counts shed some light on the situation, and uncover other potential issues with the data and/or the data collection protocol.

			Total			
		Yes	No	99	(blank)	Total
	Male	1	17	1	0	19
Sex	Female	6	9	0	2	17
•	(blank)	0	1	0	1	2
	Total	7	27	1	3	38

One of the green entries is actually blank along the two variables; depending on the other information, this entry could be a candidate for **imputation** or outright **deletion** (more on these concepts in the next section).

Three other observations are missing a value along exactly one variable, but the information provided by the other variables may be complete enough to warrant imputation. Of course, if more information is available about the patients, the analyst may be able to determine why the values were missing in the first place (however privacy concerns at the collection stage might muddy the waters).

The mis-coded information on the pregnancy status (99, in yellow) is linked to a male client, and as such re-coding it as 'No' is likely to be a reasonable decision.⁴

A similar reasoning process should make the analyst question the validity of the entry shaded in red – it might very well be correct, but it is important to at least inquire about this data point, as the answer could lead to an eventual re-framing of the definitions and questions used at the collection stage.

In general, there is no universal or one-size-fits-all approach – a lot depends on the **nature of the data**. As always, domain expertise can provide valuable help and suggest fruitful exploration avenues.

^{4:} Although this may not necessarily be the correct decision... data measurements are rarely as clear cut as we may think upon only a first reflection.

15.4 Missing Values

Obviously, the best way to treat missing data is not to have any (T. Orchard, M. Woodbury, [178]).

Why does it matter that some values may be missing?

As a start, missing values can potentially introduce **bias** into the analysis, which is rarely (if at all) a good thing, but, more pragmatically, they may interfere with the functioning of most analytical methods, which cannot easily accommodate missing observations without breaking down.⁵

Consequently, when faced with missing observations, analysts have two options: they can either **discard** the missing observation (which is not typically recommended, unless the data is missing completely randomly), or they can **create a replacement value** for the missing observation (the **imputation** strategy has drawbacks since we can never be certain that the replacement value is the true value, but is often the best available option; information in this section is taken partly from [179–182]).

Blank fields come in 4 flavours:

- nonresponse an observation was expected but none was entered;
- data entry issues an observation was recorded but was not entered in the dataset;
- invalid entries an observation was recorded but was considered invalid and has been removed, and
- **expected blanks** a field has been left blank, but expectedly so.

Too many missing values of the first three types can be indicative of **issues with the data collection process**, while too many missing values of the fourth type can be indicative of **poor questionnaire design** (see [183] for a brief discussion on these topics).

Either way, missing values cannot simply be ignored: either the

- corresponding record is removed from the dataset (not recommended without justification, as doing so may cause a loss of auxiliary information and may bias the analysis results), or
- missing values must be imputed (that is to say, a reasonable replacement value must be found).⁶

15.4.1 Missing Value Mechanisms

The relevance of an imputation method is dependent on the underlying **missing value mechanism**. Indeed, values may be:

- missing completely at random (MCAR) the item absence is independent of its value or of the unit's auxiliary variables (e.g., an electrical surge randomly deletes an observation in the dataset);
- missing at random (MAR) the item absence is not completely random, and could, in theory, be accounted by the unit's complete auxiliary information, if available (e.g., if women are less likely to tell you their age than men for societal reasons, but not because of the age values themselves), and

5: As an example, the normal equations $X^T X \beta = X^T Y$ of linear regression could not be solved if some of the data is missing as $X^T X$ is not defined in that case.

6: A non-negligible proportion of stakeholders, who would be the first to tell you that they understand nothing about data analysis in the first place, balk at this notion. It helps to remember that we do not generally conduct data analysis to fully understand any particular unit/observation, but rather to get a sense for overall patterns in the data (and how we could use these patterns to make predictions for the future, say). We suspect that this is directly linked to the fear that our "personhood" will be erased in favour of numerical summaries, that we are who the data says we are instead of ... well, who we really are. Measurement errors happen.

• not missing at random (NMAR) – the reason for nonresponse is related to the item value itself (e.g., if illicit drug users are less likely to admit to drug use than teetotallers).

The analyst's main challenge in that regard is that the missing mechanism cannot typically be determined with **any degree of certainty**.

15.4.2 Imputation Methods

There are numerous statistical **imputation** methods. They each have their strengths and weaknesses; analysts should take care to select a method which is appropriate for the situation at hand.⁷

- In **list-wise deletion**, all units with at least one missing value are removed from the dataset. This straightforward imputation strategy assumes MCAR, but it can introduce bias if MCAR does not hold, and it leads to a reduction in the sample size and an increase in standard errors.
- In mean or most frequent imputation, the missing values are substituted by the average or most frequent value in the unit's subpopulation group (stratum). This commonly-used approach also assumes MCAR, but it can create distortions in the underlying distributions (such as a spike at the mean) and create spurious relationships among variables.
- In regression or correlation imputation, the missing values are substituted using a regression on the other variables. This model assumes MAR and trains the regression on units with complete information, in order to take full advantage of the auxiliary information when it is available. However, it artificially reduces data variability and produces over-estimates of correlations.
- In stochastic regression imputation, the regression estimates are augmented with random error terms added. Just as in regression estimation, the model assumes MAR; an added benefit is that it tends to produce estimates that "look" more realistic than regression imputation, but it comes with an increased risk of type I error (false positives) due to small standard errors.
- Last observation carried forward (LOCF) and its cousin next observation carried backward (NOCB) are useful for longitudinal data; a missing value can simply be substituted by the previous or next value. LOCF and NOCB can be used when the values do not vary greatly from one observation to the next, and when values are MCAR. Their main drawback is that they may be too "generous" for studies that are trying to determine the effect of a treatment over time, say.
- Finally, in *k*-nearest-neighbour imputation, a missing entry in a MAR scenario is substituted by the average (or median, or mode) value from the subgroup of the *k* most similar complete respondents. This requires a notion of **similarity** between units (which is not always easy to define reasonably). The choice of *k* is somewhat arbitrary and can affect the imputation, potentially distorting the data structure when it is too large.

What does imputation look like in practice? Consider the following scenario (which is, somewhat embarrassingly, based on a true story).

7: Imputation methods work best under MCAR or MAR, but keep in mind that they all tend to produce **biased estimates** nonetheless... the hope is the bias is small, and that the benefits of obtaining an estimate in the first place overcomes the presence of bias.

Example: after marking the final exams of the 211 students who did not drop her course in *Advanced Retroencabulation* at State University, Dr. Helga Vanderwhede creates a data frame grades of final exam grades and mid term-grades.

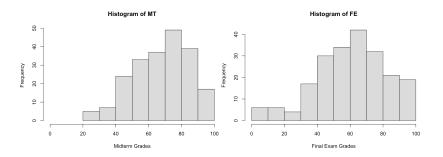
```
Setting up the grades data frame
MT = c(
80,73,83,60,49,96,87,87,60,53,66,83,32,80,66,90,72,55,76,
46,48,69,45,48,77,52,59,97,76,89,73,73,48,59,55,76,87,55,
80,90,83,66,80,97,80,55,94,73,49,32,76,57,42,94,80,90,90,
62,85,87,97,50,73,77,66,35,66,76,90,73,80,70,73,94,59,52,
81,90,55,73,76,90,46,66,76,69,76,80,42,66,83,80,46,55,80,
76,94,69,57,55,66,46,87,83,49,82,93,47,59,68,65,66,69,76,
38,99,61,46,73,90,66,100,83,48,97,69,62,80,66,55,28,83,59,
48,61,87,72,46,94,48,59,69,97,83,80,66,76,25,55,69,76,38,
21,87,52,90,62,73,73,89,25,94,27,66,66,76,90,83,52,52,83,
66,48,62,80,35,59,72,97,69,62,90,48,83,55,58,66,100,82,78,
62,73,55,84,83,66,49,76,73,54,55,87,50,73,54,52,62,36,87,
80,80
)
FE = c(
41,54,93,49,92,85,37,92,61,42,74,84,61,21,75,49,36,62,92,
85,50,90,52,63,64,85,66,51,41,75,4,46,38,71,42,18,76,42,
94,53,77,65,95,3,74,0,97,62,74,61,80,47,39,92,59,37,59,71,
20,67,69,88,53,52,81,41,81,48,67,65,92,75,68,55,67,51,83,
71,58,37,65,66,51,43,83,34,55,59,20,62,22,70,64,59,73,74,
73,53,44,36,62,45,80,85,41,80,84,44,73,72,60,65,78,60,34,
91,40,41,54,91,49,92,85,37,92,61,42,74,84,61,21,75,49,36,
62,92,85,50,92,52,63,64,85,66,51,41,75,4,46,38,71,42,18,
76,42,92,53,77,65,92,3,74,0,52,62,74,61,80,47,39,92,59,37,
59,71,20,67,69,88,53,52,81,41,81,48,67,65,94,75,68,55,67,
51,83,71,58,37,65,66,51,43,83,34,55,59,20,62,22,70,64,59
)
grades=data.frame(MT,FE)
summary(grades)
```

MT	FE
Min.: 21.0	Min.: 0.00
1st Qu.: 55.00	1st Qu.: 56.50
Median: 70.00	Median: 62.00
Mean: 68.74	Mean: 60.09
3rd Qu.: 82.50	3rd Qu.: 75.00
Max.: 100.00	Max.: 97.00

She plots the final exam grades (y) against the mid-term exam grades (x), as seen below.

Plotting the grades data frame I

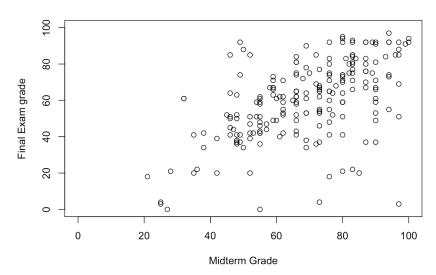
```
hist(MT, xlim=c(0,100), xlab=c("Midterm Grades"))
hist(FE, xlim=c(0,100), xlab=c("Final Exam Grades"))
```



Plotting the grades data frame II

```
plot(grades, xlim=c(0,100), ylim=c(0,100),
      xlab=c("Midterm Grade"), ylab=c("Final Exam grade"),
      main=c("Course Results"))
```

Course Results



Looking at the data, she sees that final exam grades are **weakly correlated** with mid-term exam grades: students who performed well on the mid-term tended to perform well on the final, and students who performed poorly on the mid-term tended to perform poorly on the final (as is usually the case), but the link is not that strong.

Correlation between mid-term and final grades

cor(grades\$MT,grades\$FE)

[1] 0.5481776

She also sees that there is a **fair amount of variability** in the data: the noise is not very tight around the (eye-balled) line of best fit. The linear regression model is:

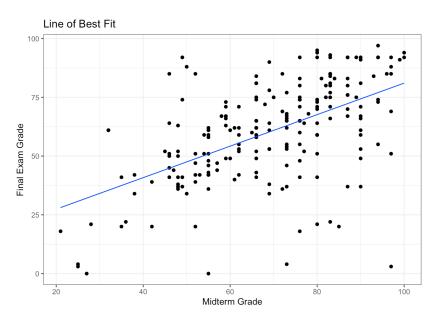
Line of best fit model <- lm(FE ~ MT, data=grades) summary(model) library(ggplot2) ggplot(model) + geom_point(aes(x=MT, y=FE)) + geom_line(aes(x=MT, y=.fitted), color="blue") + theme_bw() + xlab(c("Midterm Grade")) + ylab(c("Final Exam Grade")) + ggtitle(c("Line of Best Fit"))</pre>

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 14.00968    5.01523    2.793    0.0057 **

MT         0.67036    0.07075    9.475    <2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 17.81 on 209 degrees of freedom Multiple R-squared: 0.3005, Adjusted R-squared: 0.2972 F-statistic: 89.78 on 1 and 209 DF, p-value: < 2.2e-16



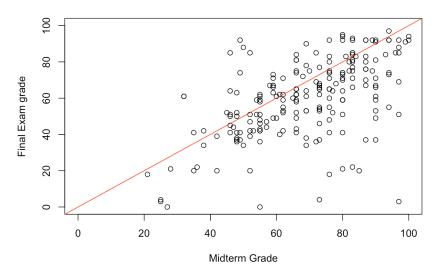
Furthermore, she realizes that the final exam was harder than the students expected (as the slope of the line of best fit is smaller than 1, as only 29% of observations lie above the line MT=FE) – she suspects that they simply did not prepare for the exam seriously, 8 as most of them could not match their mid-term exam performance.

8: And not that she made the exam too difficult, no matter what her ratings on RateMyProfessor.com suggest.

```
sum(grades$MT <= grades$FE)/nrow(grades)</pre>
```

```
plot(grades, xlim=c(0,100), ylim=c(0,100),
     xlab=c("Midterm Grade"), ylab=c("Final Exam grade"),
     main=c("Course Results"))
abline(a=0, b=1, col="red")
```

Course Results



As Dr. Vanderwhede comes to terms with her disappointment, she takes a deeper look at the numbers, at some point sorting the dataset according to the mid-term exam grades.

```
s.grades <- grades[order(-grades$MT),]
head(s.grades,16)</pre>
```

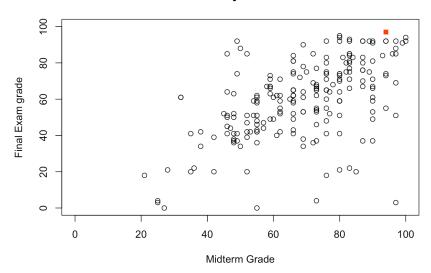
student	MT	FE
122	100	92
188	100	94
116	99	91
28	97	51
44	97	3
61	97	69
125	97	92
143	97	85
179	97	88
6	96	85
*47	94	97
54	94	92
74	94	55
97	94	73
139	94	92
162	94	74

It looks like good old Mary Sue (row number 47) performed better on the final than on the mid-term (where her performance was already superlative), scoring the highest grade. What a great student she is!⁹

```
plot(s.grades[,c("MT","FE")], xlim=c(0,100), ylim=c(0,100),
    col=ifelse(row.names(s.grades)=="47",'red','black'),
    pch=ifelse(row.names(s.grades)=="47",22,1), bg='red',
    xlab=c("Midterm Grade"), ylab=c("Final Exam grade"),
    main=c("Mary Sue!"))
```

9: And such a fantastic person – in spite of her superior intellect, she is adored by all of her classmates, thanks to her sunny disposition and willingness to help at all times. If only all students were like Mary Sue...

Mary Sue!



She continues to toy with the spreadsheet until the phone rings. After a long and exhausting conversation with Dean Bitterman about teaching loads and State University's reputation, Dr. Vanderwhede returns to the spreadsheet and notices in horror that she has accidentally deleted the final exam grades of all students with a mid-term grade greater than 93.

```
s.grades$FE.NA <- ifelse(s.grades$MT>93,NA,s.grades$FE)
```

What is she to do? Anyone with a modicum of technical savvy would advise her to either undo her changes or to close the file without saving the changes, ¹⁰ but in full panic mode, the only solution that comes to her mind is to impute the missing values.

She knows that the missing final grades are MAR (and not MCAR since she remembers sorting the data along the MT values); she produces the imputations shown in Figure 15.4.

```
List-wise deletion

plot(s.grades[,c("MT","FE.NA")], xlim=c(0,100),
    ylim=c(0,100), xlab=c("Midterm Grade"),
    ylab=c("Final Exam grade"),
```

main=c("List-wise Deletion"))

10: Or to simply re-enter the final grades by comparing with the physical papers...

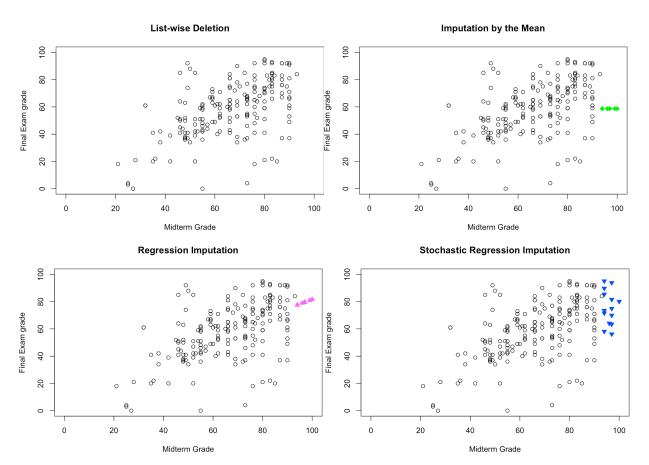


Figure 15.4: Imputation results in the grades data frame: listwise deletion (top left), mean imputation (top right), regression imputation (bottom left), stochastic regression imputation (bottom right).

Regression imputation

```
model.2 <- lm(FE.NA ~ MT, data=s.grades)
s.grades$FE.NA.reg <- ifelse(s.grades$MT>93,
    model.2[[1]][1]+model.2[[1]][2]*s.grades$MT,
    s.grades$FE)
plot(s.grades[,c("MT","FE.NA.reg")], xlim=c(0,100),
    ylim=c(0,100), pch=ifelse(s.grades$MT>93,24,1),
    col=ifelse(s.grades$MT>93,'magenta','black'),
    bg='magenta', xlab=c("Midterm Grade"),
    ylab=c("Final Exam grade"),
    main=c("Regression Imputation"))
```

Stochastic regression imputation

```
model.3 <- lm(FE.NA ~ MT, data=s.grades)
s.grades$FE.NA.sreg <- ifelse(s.grades$MT>93,
    model.3[[1]][1]+model.3[[1]][2]*s.grades$MT +
    rnorm(nrow(s.grades),0,summary(model.3)$sigma),
    s.grades$FE)
plot(s.grades[,c("MT","FE.NA.sreg")], xlim=c(0,100),
    ylim=c(0,100), pch=ifelse(s.grades$MT>93,25,1),
    col=ifelse(s.grades$MT>93,'blue','black'),
    bg='blue', xlab=c("Midterm Grade"),
    ylab=c("Final Exam grade"),
    main=c("Stochastic Regression Imputation"))
```

She remembers what the data looked like originally, and concludes that the best imputation method is the stochastic regression model.

This conclusion only applies to this specific example, however. In general, that might not be the case due to various *No Free Lunch* results.¹¹

The main take-away from this example is that various imputation strategies lead to different outcomes, and perhaps more importantly, that even though the imputed data might "look" like the true data, we have no way to measure its **departure from reality** – any single imputed value is likely to be completely off.

Mathematically, this might not be problematic, as the average departure is likely to be relatively small, but in a business context or a personal one, this might create gigantic problems – how is Mary Sue likely to feel about Dr.Vanderwhede's solution to her conundrum?

student	MT	FE	FE.NA.reg		
*47	94	97	77.54035		

And how would Dean Bitterman react were he to find out about the imputation scenario from irate students? The solution has to be compatible with the ultimate data science objective: from Dr. Vanderwhede's perspective, perhaps the only thing that matters is capturing the **essence** of the students' performance, but from the student's perspective, the objective is emphatically different.¹²

Even though such questions are not quantitative in nature, their answer will impact any actionable solution.

15.4.3 Multiple Imputation

Another drawback of imputation is that it tends to increase the noise in the data, because the imputed data is treated as the *actual* data.

11: "There ain't no such thing as a free lunch" – there is no guarantee that a method that works best for a dataset works even reasonably well for another.

12: Analysts cannot simply hide their heads in the sand on this topic: if the data science objectives are incompatible with the units' well-being, it is the objectives that need to change – we cannot ask the entities represented by those units to "get over it".

In **multiple imputation**, the impact of that noise can be reduced by consolidating the analysis outcome from multiple imputed datasets. Once an imputation strategy has been selected on the basis of the (assumed) missing value mechanism,

- 1. the imputation process is repeated *m* times to produce *m* versions of the dataset (assuming a stochastic procedure if the imputed dataset is always the same, this procedure is worthless);
- 2. each of these datasets is analyzed, yielding *m* outcomes, and
- 3. the *m* outcomes are pooled into a single result for which the mean, variance, and confidence intervals are known.

On the plus side, multiple imputation is **easy to implement**, **flexible**, as it can be used in a most situations (MCAR, MAR, even NMAR in certain cases), and it accounts for **uncertainty** in the imputed values.

However, *m* may need to be quite **large** when the values are missing in large quantities from many of the dataset's features, which can substantially slow down the analyses.

There may also be additional technical challenges when the output of the analyses is not a single value but some more complicated object. A generalization of multiple imputation was used by Transport Canada to predict the Blood Alcohol Level (BAC) content level in fatal traffic collisions that involved pedestrians [184].

15.5 Anomalous Observations

The most exciting phrase to hear [...], the one that heralds the most discoveries, is not "Eureka!" but "That's funny..." [I. Asimov (attributed)].

Outlying observations are data points which are **atypical** in comparison to the unit's remaining features (*within-unit*), or in comparison to the measurements for other units (*between-units*), or as part of a collective subset of observations. Outliers are thus observations which are **dissimilar to other cases** or which contradict **known dependencies**/rules.¹³

Note that observations could be anomalous in one context, but not in another. Consider, for instance, an adult male who is 6 feet tall. Such a man would fall in the 86th percentile among Canadian males [185], which, while on the tall side, is not unusual; in Bolivia, however, the same man would land in the 99.9th percentile [185], which would mark him as extremely tall and quite dissimilar to the rest of the population.¹⁴

A common mistake that analysts make when dealing with outlying observations is to remove them from the dataset without carefully studying whether they are **influential data points**, that is, observations whose absence leads to **markedly different** analysis results.

When influential observations are identified, remedial measures (such as data transformation strategies) may need to be applied to minimize any undue effect. Outliers may be influential, and influential data points may be outliers, but the conditions are neither necessary nor sufficient.

- 13: Outlying observations may be anomalous along any of the individual variables, or in combination.
- 14: Anomaly detection points towards interesting questions for analysts and subject matter experts: in this case, why is there such a large discrepancy in the two groups?

15.5.1 Anomaly Detection

By definition, anomalies are **infrequent** and typically surrounded by **uncertainty** due to their relatively low numbers, which makes it difficult to differentiate them from banal **noise** or **data collection errors**.

Furthermore, the boundary between normal and deviant observations is usually **fuzzy**; with the advent of e-shops, for instance, a purchase which is recorded at 3AM local time does not necessarily raise a red flag anymore.

When anomalies are actually associated to **malicious activities**, they are more than often **disguised** in order to blend in with normal observations, which obviously complicates the detection process.

Numerous methods exist to identify anomalous observations; **none of them are foolproof** and judgement must be used. Methods that employ graphical aids (such as box-plots, scatterplots, scatterplot matrices, and 2D tours) to identify outliers are particularly easy to implement, but a low-dimensional setting is usually required for ease of interpretation.

Analytical detection methods also exist (using Cooke's or Mahalanobis' distances, for instance), but in general some additional level of analysis must be performed, especially when trying to identify influential points (cf. leverage, Chapter 8, Classical Regression Analysis).

With small datasets, anomaly detection can be conducted on a case-by-case basis, but with large datasets, the temptation to use **automated detection/removal** is strong – care must be exercised before the analyst decides to go down that route.¹⁵

In the early stages of anomaly detection, **simple data analyses** (such as descriptive statistics, 1- and 2-way tables, and traditional visualizations) may be performed to help identify anomalous observations, or to obtain insights about the data, which could eventually lead to modifications of the analysis plan.

15: This stems partly from the fact that once the "anomalous" observations have been removed from the dataset, previously "regular" observations can become anomalous in turn in the smaller dataset; it is not clear when that runaway train will stop.

15.5.2 Outlier Tests

How are outliers *actually* detected? Most methods come in one of two flavours: **supervised** and **unsupervised** (we will discuss those in detail in later sections).

Supervised methods use a historical record of **labeled** (that is to say, previously identified) anomalous observations to build a **predictive classification or regression model** which estimates the probability that a unit is anomalous; domain expertise is required to tag the data.

Since anomalies are typically **infrequent**, these models often also have to accommodate the **rare occurrence problem**. ¹⁶

Unsupervised methods, on the other hand, use no previously labeled information or data, and try to determine if an observation is an outlying one solely by comparing its behaviour to that of the other observations. The following traditional methods and tests of outlier detection fall into this category:¹⁷

16: Supervised models are built to minimize a cost function; in default settings, it is often the case that the mis-classification cost is assumed to be symmetrical, which can lead to technically correct but useless solutions. For instance, the vast majority (99.999+%) of air passengers emphatically do not bring weapons with them on flights; a model that predicts that no passenger is attempting to smuggle a weapon on board a flight would be 99.999+% accurate, but it would miss the point completely.

17: Note that **normality** of the underlying data is an assumption for most tests; how robust these tests are against departures from this assumption depends on the situation.

 Perhaps the most commonly-used test is Tukey's boxplot test; for normally distributed data, regular observations typically lie between the inner fences

$$Q_1 - 1.5(Q_3 - Q_1)$$
 and $Q_3 + 1.5(Q_3 - Q_1)$.

Suspected outliers lie between the inner fences and their respective **outer fences**

$$Q_1 - 3(Q_3 - Q_1)$$
 and $Q_3 + 3(Q_3 - Q_1)$.

Points beyond the outer fences are identified as **outliers** (Q_1 and Q_3 represent the data's 1st and 3rd quartile; see Figure 15.5).

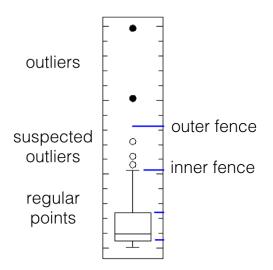
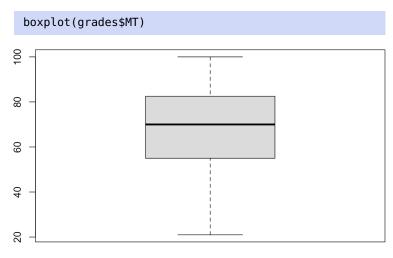


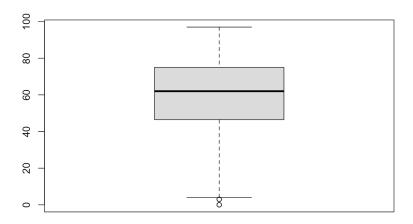
Figure 15.5: Tukey's boxplot test; suspected outliers are marked by white disks, outliers by black disks [author unknown].

As an example, let's find the outliers for the midterm and final exam grades in Dr. Vanderwhede's *Advanced Retroencabulation* course. There are no boxplot anomalies for midterm grades:



but there are 4 boxplot anomalies for final exam grades:

boxplot(grades\$FE)
boxplot.stats(grades\$FE)\$out



[1] 3 0 3 0

The corresponding observations can be found as follows:

```
out <- boxplot.stats(grades$FE)$out
out_ind <- which(grades$FE %in% c(out))
grades[out_ind,]</pre>
```

student	MT	FE	student	MT	FE
44	97	3	161	25	3
46	55	0	163	27	0

■ The **Grubbs test** is another univariate test, which takes into consideration the number of observations in the dataset. Let x_i be the value of feature X for the i^{th} unit, $1 \le i \le N$, let (\overline{x}, s_x) be the mean and standard deviation of feature X, let α be the desired significance level, and let $T(\alpha, N)$ be the critical value of the Student t-distribution at significance $\alpha/2N$. Then, the i^{th} unit is an **outlier along feature** X if

$$|x_i - \overline{x}| \ge \frac{s_x(N-1)}{\sqrt{N}} \sqrt{\frac{T^2(\alpha, N)}{N - 2 + T^2(\alpha, N)}}.$$

- Other common tests include:
 - the **Mahalanobis distance**, which is linked to the leverage of an observation (a measure of influence), can also be used to find multi-dimensional outliers, when all relationships are linear (or nearly linear);
 - the **Tietjen-Moore** test, which is used to find a specific number of outliers;
 - the **generalized extreme studentized deviate** test, if the number of outliers is unknown;
 - the **chi-square** test, when outliers affect the goodness-of-fit, as well as
 - DBSCAN and other clustering-based outlier detection methods

We will have a lot more to say on the topic in Chapter 27 (*Anomaly Detection and Outlier Analysis*).

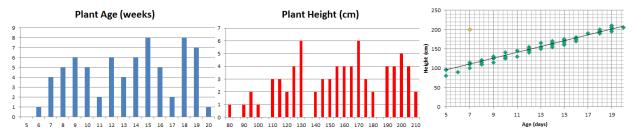


Figure 15.6: Summary visualisations for an artificial plant dataset: age distribution (left), height distribution (middle), height vs. age, with linear trend (right).

15.5.3 Visual Outlier Detection

The following three (simple) examples illustrate the principles underlying visual outlier and anomaly detection.

Example: On a specific day, the height of several plants are measured. The records also show each plant's age (the number of weeks since the seed has been planted).

Histograms of the data are shown in Figure 15.6 (age on the left, height in the middle).

Very little can be said about the data at that stage: the age of the plants (controlled by the nursery staff) seems to be somewhat haphazard, as does the response variable (height). A scatter plot of the data (rightmost chart in Figure 15.6), however, reveals that growth is strongly correlated with age during the early period of a plant's life for the observations in the dataset; points clutter around a linear trend. One point (in yellow) is easily identified as an **outlier**.

There are (at least) two possibilities: either that measurement was botched or mis-entered in the database (representing an invalid entry), or that one specimen has experienced unusual growth (outlier). Either way, the analyst has to investigate further.

Example: a government department has 11 service points in a jurisdiction. Service statistics are recorded: the monthly average arrival rates per teller and average service rates per teller are available for each service point.

A scatter plot of the service rate per teller (y axis) against the arrival rate per teller (x axis), with linear regression trend, is shown in the leftmost chart in Figure 15.7. The trend inches upwards with increasing x values.

A similar chart, but with the left-most point removed from consideration, is shown in the middle chart of Figure 15.7. The trend still slopes upward, but the fit is significantly improved, suggesting that the removed observation is unduly **influential** (or anomalous) – a better understanding of the relationship between arrivals and services is afforded if it is set aside.

Any attempt to fit that data point into the model must take this information into consideration. Note, however, that influential observations depend on the analysis that is ultimately being conducted – a point may be influential for one analysis, but not for another.

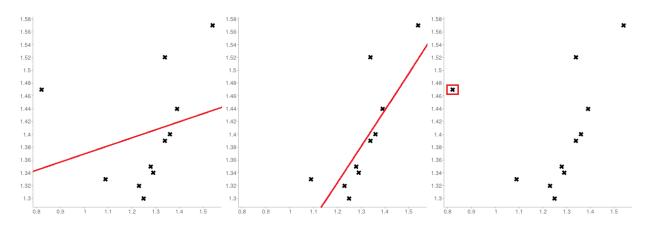


Figure 15.7: Visualisations for an (artificial) service point dataset: trend for 11 service points (left), trend for 10 service points (middle), influential observations (right).

Example: measurements of the length of the appendage of a certain species of insect have been made on 71 individuals. Descriptive statistics have been computed; the results are shown in Table 15.5.

Appendage length (mm)						
Mean	10.35					
Standard Deviation	16.98					
Kurtosis	16.78					
Skewness	4.07					
Minimum	0					
First Quartile	0					
Median	8.77					
Third Quartile	10.58					
Maximum	88					
Range	88					
Interquartile Range	10.58					
Mode	0					
Count	71					

Table 15.5: Descriptive statistics for an (artificial) appendage length dataset.

Analysts who are well-versed in statistical methods might recognize the tell-tale signs that the distribution of appendage lengths is likely to be asymmetrical and to have a "fat" tail. 18

The mode, minimum, and first quartile values belong to individuals without appendages, so there appears to be at least two sub-groups in the population (perhaps split along the lines of juveniles/adults, or males/females).

The maximum value has already been seen to be quite large compared to the rest of the observations, which at first suggests that it might belong to an **outlier**.

The histogram of the measurements, however, shows that there are 3 individuals with very long appendages (see the chart in Figure 15.8): it now becomes plausible for these anomalous entries to belong to individuals from a different species altogether who were **erroneously added** to the dataset. This does not, of course, constitute a proof of such an error, but it raises the possibility, which is often the best that an analyst can do in the absence of subject matter expertise.

18: Since the skewness is non-negligible, and due to the kurtosis being commensurate with the mean and the standard deviation, the range being so much larger than the interquartile range, and the maximum value being so much larger than the third quartile.

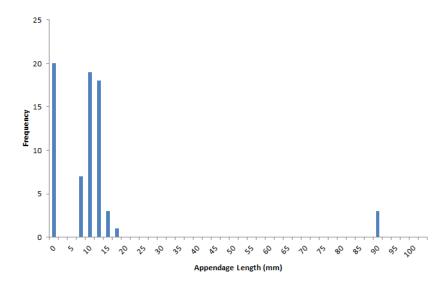


Figure 15.8: Frequency chart of the appendage lengths in the artificial dataset.

15.6 Data Transformations

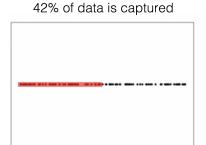
History is the transformation of tumultuous conquerors into silent footnotes. [P. Eldridge]

This **crucial** step is often neglected or omitted altogether. Various transformation methods are available, depending on the analysts' needs and data types, including:

- standardization and unit conversion, which put the dataset's variables on an equal footing – a requirement for basic comparison tasks and more complicated problems of clustering and similarity matching;
- normalization, which attempts to force a variable into a normal distribution – an assumption which must be met in order to use number of traditional analysis methods, such as ANOVA or regression analysis, and
- smoothing methods, which help remove unwanted noise from the data, but at a price – perhaps removing natural variance in the data.

Another type of data transformation is pre-occupied with the concept of **dimensionality reduction**. There are many advantages to working with low-dimensional data:

- visualization methods of all kinds are available to extract and present insights out of such data;
- high-dimensional datasets are subject to the so-called curse of dimensionality, which asserts (among other things) that multidimensional spaces are vast, and when the number of features in a model increases, the number of observations required to maintain predictive power also increases, but at a substantially higher rate (see Figure 15.9),
- another consequence of the curse is that in high-dimension sets, all
 observations are roughly dissimilar to one another observations
 tend to be nearer the dataset's boundaries than they are to one
 another.



14% of data is captured

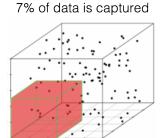


Figure 15.9: Illustration of the curse of dimensionality; N = 100 observations are uniformly distributed on the unit hypercube $[0,1]^d$, d = 1,2,3. The red regions represent the smaller hypercubes $[0,0.5]^d$, d = 1,2,3. The percentage of captured datapoints is seen to decrease with an increase in d [186].

Dimension reduction techniques such as:

- principal component analysis, independent component analysis, and factor analysis for numerical data, or
- multiple correspondence analysis for categorical data

project multi-dimensional datasets onto low-dimensional but high information spaces;¹⁹ feature selection techniques, including the popular family of **regularization methods** (see Chapter 20, *Regression and Value Estimation*) select an **optimal subset of variables** with which to accomplish tasks, according to some appropriate, context-dependent criterion.

Some information is necessarily lost in the process, but in many instances the drain can be kept under control and the gains made by working with smaller datasets can offset the losses of completeness. We will have more to say on the topic in Chapter 23 (\emph{Feature Selection and Dimension Reduction).

19: The so-called Manifold Hypothesis.

15.6.1 Common Transformations

Models often require that certain data assumptions be met. For instance, ordinary least square regression assumes:

- that the response variable is a **linear combination** of the predictors;
- constant error variance;
- uncorrelated residuals, which may or may not be statistically independent,
- etc.

In reality, it is rare that raw data meets all these requirements, but that does not necessarily mean that we need to abandon the model – an **invertible** sequence of data transformations may produce a derived data set which *does* meet the requirements, allowing the consultant to draw conclusions about the original data.

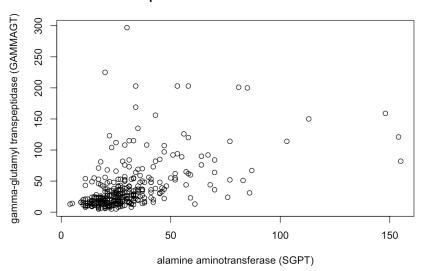
In the regression context, invertibility is guaranteed by **monotonic** transformations: identity, logarithmic, square root, inverse (all members of the power transformations), exponential, etc.

These transformations are illustrated below on a subset of the BUPA liver disease dataset [187].

Subset of the BUPA liver disease dataset

```
library(kerndwd)
data(BUPA)
plot(BUPA$X[,3],BUPA$X[,5],
    main="Scatterplot of a subset of the BUPA dataset",
    xlab="alamine aminotransferase (SGPT)",
    ylab="gamma-glutamyl transpeptidase (GAMMAGT)")
```

Scatterplot of a subset of the BUPA dataset



In Figure 15.10, we show the effect of various transformations on X = SGPT and Y = GAMMAGT.

There are rules of thumb and best practices to transform data, but analysts should not discount the importance of exploring the data visually before making a choice.

Transformations on the **predictors** X may be used to achieve the **linearity assumption**, but they usually come at a price – Pearson correlations are not preserved by such transformations, for instance.²⁰

Transformations on the target *Y* can help with **non-normality** of residuals and **non-constant variance** of error terms.

Note that transformations can be applied **both** to the target variable or the predictors: as an example, if the linear relationship between two variables X and Y is expressed as Y = a + bX, then a unit increase in X is associated with an average of b units in Y.

But a better fit might be provided by either of

$$\log Y = a + bX$$
, $Y = a + b \log X$, or $\log Y = a + b \log X$,

for which:

- a unit increase in X is associated with an average b% increase in Y;
- a 1% increase in *X* is associated with an average 0.01*b* unit increase in *Y* , and
- a 1% increase in X is associated with a b% increase in Y, respectively.

20: Spearman correlations are preserved (in magnitude) by monotonous transformations, however.

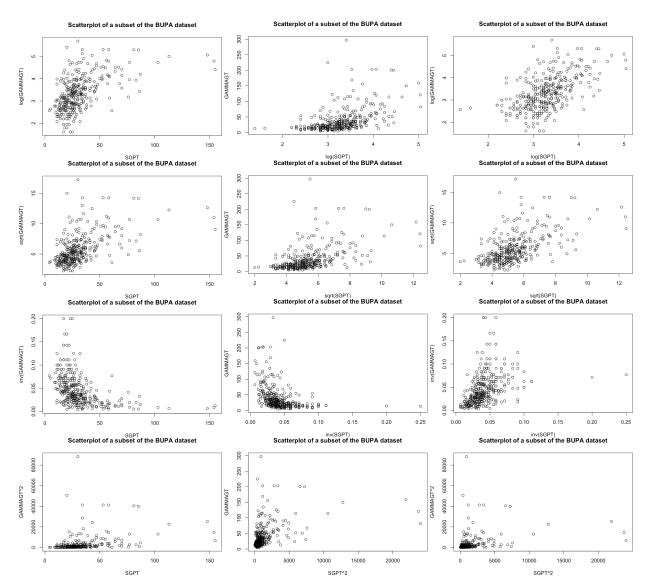


Figure 15.10: Various data transformations for a subset of the BUPA liver disease dataset [187], involving the logarithm, the square root, the inverse, and the square of both variables (see the axes for the specific transformation.

15.6.2 Box-Cox Transformations

There is a useful framework that provides an optimal transformation, in a certain sense. Consider the task of predicting the target Y with the help of the predictors X_j , $j = 1, \ldots, p$. The usual model takes the form

$$y_i = \sum_{j=1}^p \beta_j X_{x,i} + \varepsilon_i, \quad i = 1, \dots, n.$$

If the residuals are skewed, or their variance is not constant, or the trend itself does not appear to be linear, a power transformation on the response might be indicated, but if so, which one? The **Box-Cox transformation** $y_i \mapsto y_i'(\lambda), y_i > 0$ is defined by

$$y_i'(\lambda) = \begin{cases} (y_1 \dots y_n)^{1/n} \ln y_i, & \text{if } \lambda = 0\\ \frac{y_i^{\lambda} - 1}{\lambda} (y_1 \dots y_n)^{\frac{1-\lambda}{n}}, & \text{if } \lambda \neq 0 \end{cases}$$

The **suggested** choice of λ is the value that maximizes the log-likelihood

$$\mathcal{L} = -\frac{n}{2} \log \left(\frac{2\pi \hat{\sigma}^2}{(y_1 \cdots y_n)^{2(\lambda-1)/n}} + 1 \right).$$

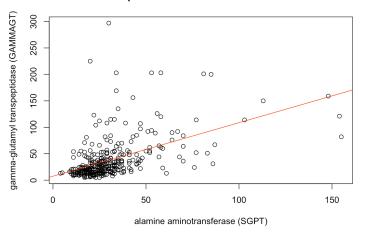
21: Assume that library(kerndwd) and data(BUPA) have already been called.

The following code shows the effect of the Box-Cox transformation on the linear fit of Y (GAMMAGT) against X (SGPT) in the BUPA dataset. ²¹

```
Linear fit in the BUPA liver disease dataset
```

```
model <- lm(BUPA$X[,5] ~ BUPA$X[,3])
plot(BUPA$X[,3],BUPA$X[,5],
    main="Scatterplot of a subset of the BUPA dataset",
    xlab="alamine aminotransferase (SGPT)",
    ylab="gamma-glutamyl transpeptidase (GAMMAGT)")
abline(a=model[[1]][1], b=model[[1]][2], col="red")</pre>
```

Scatterplot of a subset of the BUPA dataset

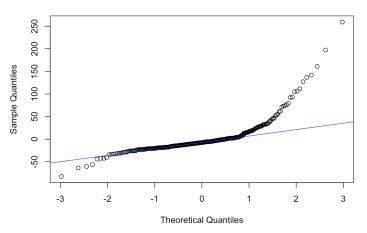


The fit looks decent, but the qq-plot of the residuals makes it clear that the normality assumption of the linear regression model is not met.

QQ plot of the untransformed BUPA model

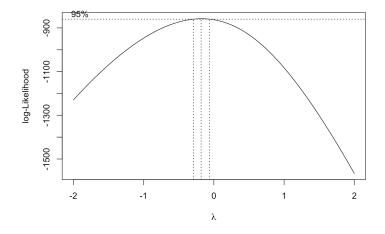
```
qqnorm(model$residuals)
qqline(model$residuals, col="blue")
```

Normal Q-Q Plot



We find the Box-Cox transformation on Y as follows:

Linear fit in the Box-Cos transformed BUPA model library(MASS) box.cox <- boxcox(BUPA\$X[,5] ~ BUPA\$X[,3]) (lambda <- box.cox\$x[which.max(box.cox\$y)])</pre>

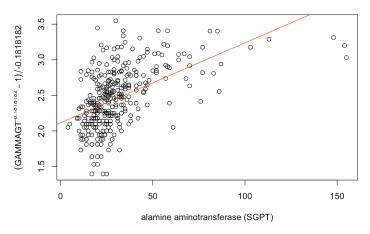


[1] -0.1818182

The linear model on the Box-Cox transformed response is given as follows.

Linear fit in the Box-Cos transformed BUPA model box.cox.Y <- (BUPA\$X[,5]^lambda-1)/lambda bc.model <- lm(box.cox.Y ~ BUPA\$X[,3]) plot(BUPA\$X[,3],box.cox.Y, main="Scatterplot of a subset of the BUPA dataset", xlab="alamine aminotransferase (SGPT)", ylab="Box-Cox response") abline(a=bc.model[[1]][1], b=bc.model[[1]][2], col="red")</pre>

Scatterplot of a subset of the BUPA dataset

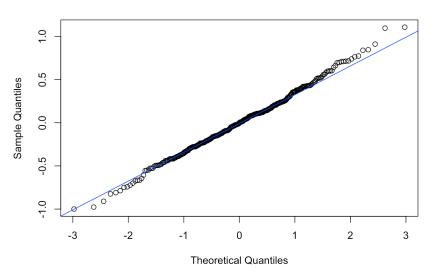


That the model on the Box-Cox data is better is evidenced by the qq-plot.

QQ plot of the transformed BUPA model

```
qqnorm(bc.model$residuals)
qqline(bc.model$residuals, col="blue")
```

Normal Q-Q Plot



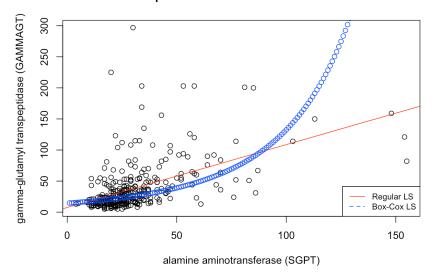
There might be theoretical rationales which favour a particular choice of λ – these are not to be ignored. It is also important to produce a residual analysis, as the best Box-Cox choice does not necessarily meet all the least squares assumptions.

Finally, it is important to remember that the resulting parameters have the least squares property **only with respect to the transformed data points** (in other words, the inverse transformation has to be applied to the results before we can make interpretations about the original data).

In the BUPA example, the corresponding curve in the untransformed space is shown below.

Linear Box-Cox model in the untransformed BUPA data

Scatterplot of a subset of the BUPA dataset



15.6.3 Scaling

Numeric variables may have different scales (weights and heights, for instance). Since the variance of a large-range variable is typically greater than that of a small-range variable, leaving the data **unscaled** may introduce biases, especially when using unsupervised methods.²²

It could also be the case that it is the relative positions (or rankings) which is of importance, in which case it could become important to look at relative distances between levels:

• **standardisation** creates a variable with mean 0 and std deviation 1:

$$Y_i = \frac{X_i - \overline{X}}{s_X},$$

• **normalization** creates a variable in the range [0, 1]:

$$Y_i = \frac{X_i - \min\{X_k\}}{\max\{X_k\} - \min\{X_k\}}.$$

There are other options; different schemes can lead to different outputs.

15.6.4 Discretizing

In order to reduce computational complexity, a numeric variable may need to be replaced with an **ordinal** variable (*height* values could be replaced by the qualitative "short", "average", and "tall", for instance.²³

It is far from obvious how to determine the bins' limits – **domain expertise** can help, but it could introduce unconscious bias to the analyses. In the absence of such expertise, limits can be set so that either the bins each:

- contain (roughly) the same number of observations;
- have the same width, or
- the performance of some modeling tool is maximized.

Again, various choices may lead to different outputs.

22: See Chapter 19, Machine Learning 101.

23: Of course, what these terms represent depend on the context; Canadian short and Bolivian tall may be fairly commensurate, to revisit the example at the start of the preceding section.

15.6.5 Creating Variables

Finally, it is possible that new variables may need to be introduced (in contrast with dimensionality reduction). These new variables may arise:

- as functional relationships of some subset of available features (introducing powers of a feature, or principal components, say);
- because the modeling tool may require independence of observations or independence of features (in order to remove multicollinearity, for instance), or
- to simplify the analysis by looking at aggregated summaries (often used in text analysis).

There is no limit to the number of new variables that can be added to a dataset – but consultants should strive for **relevant additions**.

15.7 Example: Algae Blooms

This example is based on a Case Study by L. Torgo [103]. It provides a concrete illustration of the data preparation process on a realistic dataset: algae_blooms.csv, which is also available at the UCI Machine Learning Repository [2].

The ultimate problem is to predict the occurrence of harmful algae in water samples. Torgo also uses it to highlight various aspects of **data exploration**, **data cleaning**, and R **syntax**.²⁴

Readers who would prefer to try this example on their own are invited to skip this section and head to the first exercise of Section 15.8.

15.7.1 Problem Description

The ability to monitor and perform early forecasts of various river algae blooms is crucial to control the ecological harm they can cause.

The dataset which is used to train the learning model consists of:

- chemical properties of various water samples of European rivers
- the quantity of seven algae in each of the samples, and
- the characteristics of the collection process for each sample.

What is the data science motivation for such a model? After all, we can analyze water samples to determine if various harmful algae are present or absent.

The answer is simple: chemical monitoring is **cheap** and **easy to automate**, whereas biological analysis of samples is **expensive** and **slow**.

Another answer is that analyzing the samples for harmful content does not provide a better understanding of algae **drivers**: it just tells us which samples contain algae.

24: We will continue this work in Section 20.6.

15.7.2 Loading the Data

Before we can take a look at the data and begin the process in earnest, we need to load it in the in the R workspace. If the dataset was downloaded from the UCIML repository and stored in the CSV file algae_blooms.csv, we can run the following:

It is also available in Torgo's DMwR package. As we will use some of its functions in this example, we will show how to install and load it. Unfortunately, it could not be installed directly from CRAN with the install.packages() function, as of January 2023.

Instead, we suggest doing the following:

- 1. Download the package source DMwR_0.4.1.tar.gz from the DMwR CRAN archive page ☑ (additional information about the package is also available there) and save it locally to some path (in this example, the file was saved to the folder docs/code/).
- 2. Install the following dependencies directly from CRAN:

```
install.packages(c("xts","quantmod","ROCR"))
```

The dependencies list might be different, based on the packages already installed locally; any eventual error message in the next step will inform you of the exact dependencies to install.

3. Install DMwR from the package source:

4. Load the package and prepare the data:

Either way, we can get a sense for the data frame's structure by calling the str function.

```
str(algae_blooms)
```

```
data.frame': 340 obs. of 18 variables:
$ season: Factor w/ 4 levels "winter" "spring" "autumn" "spring" ...
$ size : Factor w/ 3 levels "small" "small" "small" "small" "small" ...
$ speed : Factor w/ 3 levels "medium" "medium" "medium" "medium" ...
$ mxPH : num  8 8.35 8.1 8.07 8.06 8.25 8.15 8.05 8.7 7.93 ...
$ mn02 : num  9.8 8 11.4 4.8 9 13.1 10.3 10.6 3.4 9.9 ...
$ Cl : num  60.8 57.8 40 77.4 55.4 ...
$ N03 : num  6.24 1.29 5.33 2.3 10.42 ...
```

```
$ NH4
               578 370 346.7 98.2 233.7 ...
        : num
               105 428.8 125.7 61.2 58.2 ...
$ oP04
        : num
$ P04
               170 558.8 187.1 138.7 97.6 ...
        : num
$ Chla
         num
               50 1.3 15.6 1.4 10.5 ...
$ a1
               0 1.4 3.3 3.1 9.2 15.1 2.4 18.2 25.4 17 ...
        : num
               0 7.6 53.6 41 2.9 14.6 1.2 1.6 5.4 0 ...
$ a2
        : num
               0 4.8 1.9 18.9 7.5 1.4 3.2 0 2.5 0 ...
$ a3
        : num
$ a4
        : num
               0 1.9 0 0 0 0 3.9 0 0 2.9 ...
               34.2 6.7 0 1.4 7.5 22.5 5.8 5.5 0 0 ...
$ a5
         num
               8.3 0 0 0 4.1 12.6 6.8 8.7 0 0 ...
$ a6
        : num
               0 2.1 9.7 1.4 1 2.9 0 0 0 1.7 ...
$ a7
          num
```

Notes:

- 3 of the fields are categorical (season, size, speed, which refer to the data collection process);
- of the numerical fields, 8 have vaguely "chemical" names;
- presumably, the remaining fields refer to the various algae blooms.

We can get a better feel for the data frame by observing it in its natural habitat, so to speak, using the head() or tail() functions.

mxPH Chla a7 season size speed а1 winter small medium 8.00 50.0 0.0 0.0 . . . spring small medium 8.35 1.3 1.4 . . . 2.1 autumn small medium 8.10 15.6 3.3 9.7 . . . medium 8.07 138.7 spring small 1.4 1.4

15.7.3 Summary and Visualization

head(algae_blooms,4)

As it happens, we are not given an awful lot of information about the dataset's **domain**.²⁵ **Data exploration**, in the form of summaries and visualization, can help provide a handle on the problem at hand.²⁶

A call to the summary function (on the next page) provides frequency counts for categorical variables, and 6-pt summaries for numerical variables. As a bonus, the number of missing values is also tabulated.²⁷

Notes:

- The *chemical* variables all have missing values, ranging from only 2 to 7, 16, and 23.
- The observations seem fairly uniformly distributed in terms of the seasons, but large rivers and low speed rivers are not represented as often as their counterparts.
- All numerical values are non-negative, which makes sense in the context of concentrations
- We do not know what the range of the chemical values *should* take in a real-world context, but some of the maximum values seem . . . unrealistic (NH4!!, oPO4, a7, etc.)
- Does anything else jump at you?

- 25: We remain woefully ill-prepared to deal with matters of a chemical nature, to our eternal shame.
- 26: **IMPORTANT NOTE:** we may have given you the impression that exploration is *only really necessary* when domain expertise escapes us. Domain expertise can help analysts frame the problem and the analysis results in the appropriate manner, but it often also gives them a false sense of security. Errors can creep anywhere data exploration at an early stage may save you a lot of embarrassing back-tracking at a later stage.
- 27: The default setting only lists a limited number of categorical levels the summary documentation will explain how to increase the number of levels that are displayed.

summary(algae_blooms)

season	au	tumn 80	spring 84		winter			
size	l	arge	medium	small	L			
		83	136	121	L			
				,				
speed	me		high					
		140	142	58	3			
	mxPH	mn0	2 Cl	N03	NH4	oP04	P04	Chla
Min.:	5.6	1.5	0.2	0.0	5.0	1.6	1.0	0.2
Q1 :	7.8	7.9	10.9	1.1	37.8	13.6	40.0	2.1
Med.:	8.0	9.7	32.4	2.3	107.3	37.2	101.5	5.1
Mean:	7.9	9.1	42.5	3.1	471.7	73.0	136.7	12.7
Q3 :	8.3	10.8	57.7	4.1	244.9	88.1	200.2	17.2
Max.:	9.7	13.4	391.5	45.6	24064.0	1435.0	1690.0	110.4
NA's:	2	2	16	2	2	2	7	23
	a1	a2	a3	a4	a5	a6	a7	
Min.:	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
Q1 :	1.5	0.0	0.0	0.0	0.0	0.0	0.0	
Med.:	7.1	2.8	1.4	0.0	2.2	0.0	0.0	
Mean:	16.7	7.2	3.9	1.8	5.5	6.4	2.2	
Q3 :	25.1	10.1	4.6	2.3	8.0	7.0	2.2	
Max.:	89.8	72.6	42.8	44.6	61.1	77.6 3	1.6	

Of course, these summaries each apply to a single variable (1-way tables). Can we find anything else using n-way tables?²⁸

28: On categorical variables, by necessity.

2-way tables

table(algae_blooms\$speed,algae_blooms\$size)
table(algae_blooms\$speed,algae_blooms\$season)
table(algae_blooms\$season,algae_blooms\$size)

	large ı	nedium s	small	
high	13	56	73	
low	32	24	2	
medium	38	56	46	
	autumn	spring	summer	winter
high	32	34	38	38
low	16	13	12	17
medium	32	37	36	35
	large ı	nedium s	small	
autumn	19	33	28	
spring	21	34	29	
summer	19	36	31	
winter	24	33	33	

3-way table

```
= high
       large medium small
autumn
           3
                 13
                        16
           3
                 14
                       17
spring
           3
                 16
                       19
summer
                       21
winter
           4
                 13
   = low
       large medium small
autumn
          9
                  6
           7
                  6
                        0
spring
summer
           6
                  6
                        0
                  6
                        1
winter
          10
  = medium
       large medium small
          7
autumn
                 14
                        11
          11
                 14
                       12
spring
summer
          10
                 14
                       12
winter
          10
                 14
                        11
```

The 6-pt summary provides some information about the underlying distribution, but not much on the parametric front. A more traditional summary can be displayed using the psych library's describe() function.

```
psych::describe(algae_blooms)
```

(the output is shown at the top of the next page)

Notes:

- the categorical variables are marked by an asterisk *; the levels are coded with an integer, and treated as numerical variables for the purpose of the analysis, so the results for these fields are meaningless
- the trimmed variable refers to the trimmed mean, the mean obtained when a certain percentage of the observations are removed from both end of the spectrum (what percentage, exactly?)
- the mad variable refers to the *median absolute deviation* (*from the median*)

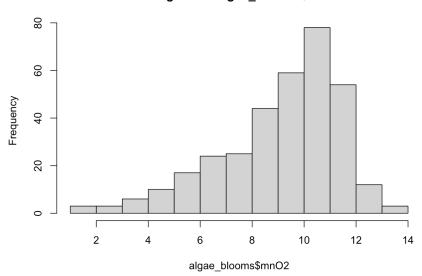
We personally find such a table hard to read and really grasp once there are more than a few variables in the dataset. **Visualization** comes in handy in such cases.

Basic histograms can be constructed with the hist() function.

	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew	kurtosis	se
season*	1	340	2.547059	1.1186895	3.0000	2.558823	1.482600	1.000	4.000	3.000	-0.0544729	-1.3652641	0.0606695
size*	2	340	2.111765	0.7676208	2.0000	2.139706	1.482600	1.000	3.000	2.000	-0.1915031	-1.2876572	0.0416301
speed*	3	340	1.994118	0.9120437	2.0000	1.992647	1.482600	1.000	3.000	2.000	0.0115387	-1.8012592	0.0494625
mxPH	4	338	7.997293	0.5783188	8.0450	8.035864	0.467019	5.600	9.700	4.100	-0.8402202	1.9865897	0.0314564
mnO2	5	338	9.156716	2.3130799	9.7000	9.388198	1.927380	1.500	13.400	11.900	-0.9392605	0.5497464	0.1258150
CI	6	324	42.517246	44.4906037	32.4700	34.997591	33.478591	0.222	391.500	391.278	2.8485675	14.0485533	2.4717002
NO3	7	338	3.120784	3.2851622	2.3555	2.699504	2.181646	0.000	45.650	45.650	6.7874378	81.1290663	0.1786893
NH4	8	338	471.734411	1739.0774580	107.3570	156.746838	119.949753	5.000	24064.000	24059.000	9.1184171	105.4980942	94.5933434
oPO4	9	338	73.091882	114.1420517	37.2430	51.792802	43.460936	1.000	1435.000	1434.000	5.9906708	60.0469965	6.2085091
PO4	10	333	136.685699	149.4773125	101.4550	115.867652	114.999352	1.000	1690.000	1689.000	4.2262442	35.1788385	8.1913063
Chla	11	317	12.796196	18.0813363	5.1110	8.782608	6.094969	0.200	110.456	110.256	2.6186753	7.8575379	1.0155490
a1	12	340	16.701765	20.9987076	7.1000	12.593750	10.526460	0.000	89.800	89.800	1.5040883	1.4996118	1.1388148
a2	13	340	7.200882	10.7549412	2.8000	4.854412	4.151280	0.000	72.600	72.600	2.3280170	6.7216331	0.5832686
a3	14	340	3.904412	6.4205247	1.4000	2.358456	2.075640	0.000	42.800	42.800	2.4150758	6.7202844	0.3482018
a4	15	340	1.810000	3.8292948	0.0000	1.036765	0.000000	0.000	44.600	44.600	5.9516431	52.8944003	0.2076727
a5	16	340	5.515588	8.4186630	2.2000	3.692279	3.261720	0.000	61.100	61.100	2.7562479	10.4260075	0.4565661
a6	17	340	6.411471	12.3978237	0.0000	3.279779	0.000000	0.000	77.600	77.600	2.8805737	9.2050442	0.6723664
a7	18	340	2.206471	4.9472217	0.0000	1.040074	0.000000	0.000	31.600	31.600	4.0903606	18.5615144	0.2683008

hist(algae_blooms\$mn02)



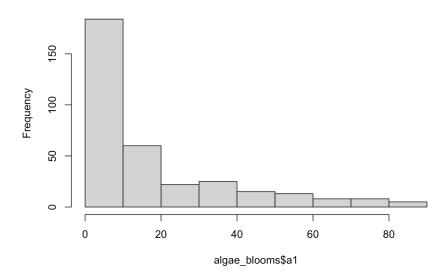


Based on this histogram, we can conclude that the underlying distribution of mn02 has a **negative skew**, say, which is confirmed by the table above.

The variable mn02 clearly does not follow a normal distribution (it never takes on negative values, and the distribution is skewed negatively, as indications); but we see that viewing it as normal would be a much better approximation than viewing the distribution of a1 as normal.

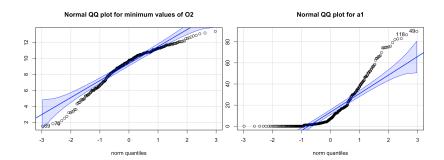
hist(algae_blooms\$a1)

Histogram of algae_blooms\$a1

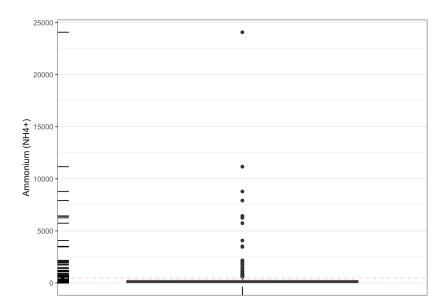


qq—plots, another traditional statistical plot, can be produced with the car library's qqPlot() function. Again, we can see that the normal distribution is not a good fit for mn02 (left), but the fit is even worse for a1 (right).

```
car::qqPlot(algae_blooms$mn02, ylab="",
    main='Normal QQ plot for minimum values of 02')
car::qqPlot(algae_blooms$a1, ylab="",
    main='Normal QQ plot for a1')
```

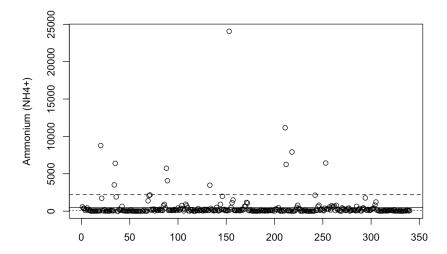


We can also take a look at some of the odd values for NH4 using ggplot2 [25, 188–190].



We see that there are a string of values falling way above the boxplot. If the underlying distribution was normal, say, these would definitely be considered outliers.

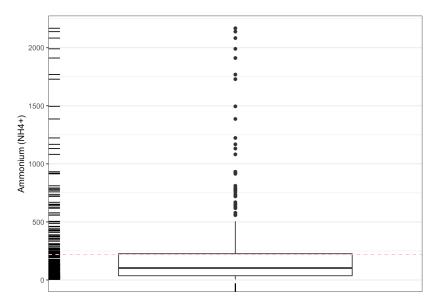
Let us investigate further.



We can also look at the data and see which observations have values of NH4 below 3000 (roughly all values below the long dashed line above).

```
nrow(algae_blooms[-which(algae_blooms$NH4>3000),])
```

What does the boxplot above looks like without the suspected outliers?

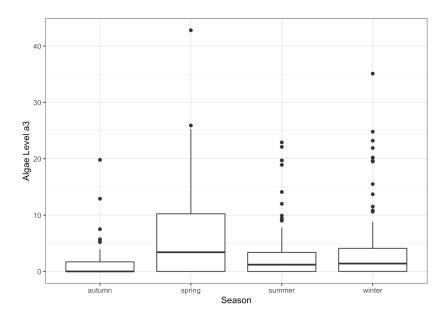


29: The box structure has expanded, and there still seems to be some very high values. Perhaps that is to be expected? How would we find out?

It is a bit better, to be sure.²⁹

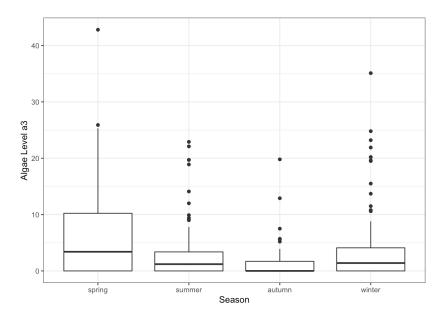
Now, let us take a look at some of the algae levels.

```
ggplot(algae_blooms,aes(x=season,y=a3)) +
geom_boxplot() + xlab("Season") + ylab("Algae Level a3")
```



What does that tell us? It is hard to get a good handle on the situation because the season are out of sequential order.

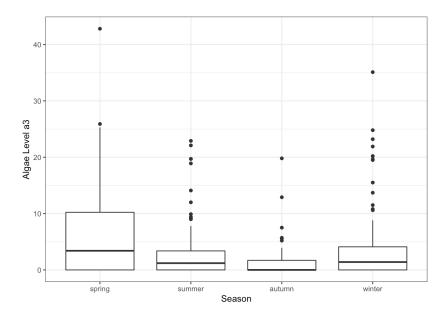
We can re-arrange the factors, but it requires a bit of fancy footwork using the forcats'library fct_relevel() function, and dplyr's mutate().



We only have 1 year's worth of data, so it might be too early to tell, but it certainly seems as though the a3 levels decrease from spring to winter.

Violin plots are cousins to the boxplots. Can we get a bit more insight on the a3 trend?

```
ggplot(algae_blooms,aes(x=season,y=a3)) +
  geom_violin() +
  geom_jitter() +
  xlab("Season") +
  ylab("Algae Level a3")
```



This plot certainly seems to suggest that a3 levels are cyclic, with a peak in the spring and low levels in the fall.

Let us return to NH4 for a second to see if we can spot a link with the season (as we did for a3). We only keep the observations for which the NH4 value is greater than 3000, and we bin them with respect to the **quartiles**.

First, filter the algae_blooms dataset to remove the 2 observations with missing values.³⁰

```
30: Remember that library(dplyr) has been called on the previous page.
```

```
f.NH4.data <- filter(algae_blooms,!is.na(NH4))
nrow(f.NH4.data)</pre>
```

[1] 338

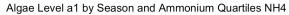
Next we remove the 11 observations for which NH4 > 3000 (again, based on the mean + sd "argument")

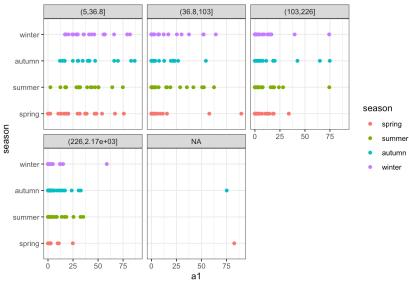
```
f.NH4.data <- filter(algae_blooms,!is.na(NH4)) |>
   filter(NH4<3000)
nrow(f.NH4.data)</pre>
```

[1] 327

We create a variable indicating in which quartile the NH4 value falls.

We can now use the new variable q.NH4 to make multi-variate comparisons, say between a1, NH4, and season.





That seems decidedly odd ... why are we seeing missing values here? Have we not just removed the NAs? Let us delve in a bit deeper.

```
f.NH4.data[which(is.na(f.NH4.data$q.NH4)),]
table(f.NH4.data$q.NH4, useNA="ifany")
```

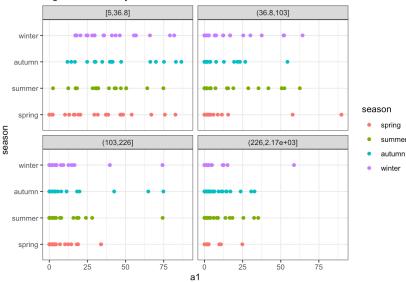
	season	size	speed	mxPH	mnO2	CI	NO3	NH4	oPO4	PO4	Chla	a1	a2	а3	a4	а5	a6	а7	q.NH4
53	spring	small	medium	5.6	11.8	NA	2.22	5	1	1	NA	82.7	0	0	0	0	0	0	NA
223	autumn	small	high	5.9	11.9	NA	1.88	5	1	2	NA	75.2	0	0	0	0	0	0	NA

Var1	Freq
(5,36.8]	80
(36.8,103]	82
(103,226]	81
(226,2.17e+03]	82
NA	2

The quartiles do not include their lower bound; we can remedy the situation by including an additional parameter in the mutate() call.

```
f.NH4.data <- filter(algae_blooms, !is.na(NH4)) |>
  filter(NH4<3000) |> mutate(q.NH4=cut(NH4,
  quantile(NH4,c(0,0.25,0.5,0.75,1)),
    include.lowest=TRUE))
```





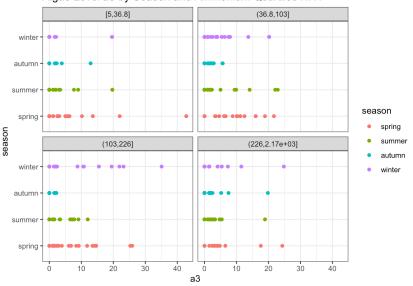
31: Although we would need more work to conclude this with any degree of certainty.

The NAs have disappeared from the graph. In any case, it seems as though the all levels are inversely correlated with the NH4 levels but that the season does not have much of an effect. 31

We can create a similar graph for a3 instead of a1.

```
ggplot(f.NH4.data,aes(x=a3,y=season,color=season)) +
   geom_point() + facet_wrap(~q.NH4) +
   ggtitle("Algae Level a3 by Season and
   Ammonium Quartiles NH4")
```

Algae Level a3 by Season and Ammonium Quartiles NH4



15.7.4 Data Cleaning

We found some potential anomalies in the data when we explored the dataset;³² now let us take some time to **clean the data** to some extent.

Anomalies come in various flavours; we have already explored some potential **outlying behaviour**, now we handle **missing values**.³³ The function complete.cases() lists the observations for which every field is present (note that it says nothing about the **validity** of the case).

```
32: Although we are electing to keep them in the dataset for the time being as we lack the domain expertise to make a reasonable decision on that front.
```

33: Again, assume that library(dplyr) has already been loaded.

```
table(complete.cases(algae_blooms))
```

Var1 Freq FALSE 34 TRUE 306

The vast majority of observations do not have missing cases, but a few still do. Is there anything special about them? Are the values missing completely at random?

```
nrow(filter(algae_blooms, !complete.cases(algae_blooms)))
summary(filter(algae_blooms, !complete.cases(algae_blooms)))
```

[1] 34

sp	ring	summer	autumn	winter	-			
	7	6	8	13	3			
ς	mall	medium	large					
3			7					
		_	•					
	low	medium	high					
	4	13	17					
mv/DII	m n O	2 (1	NOS	NILLA	o DO 4	D0.4	Chl a	
7.2			1.4	11.8	3.6	10.8	4.0	
7.3	10.1	19.3	2.1	62.0	25.6	34.5	13.9	
8.0	11.3	25.2	2.5	46.3	20.2	19.2	12.2	
9.7	12.6	71.0	11.0	500.0	295.6	380.0	68.0	
2	2	16	2	2	2	7 2	23	
_		_		_	_	_		
0.0	0.0	0.0	0.0	0.0		0.0		
16.8	0.0	0.0	0.0	0.0	0.0	0.0		
30.3	0.0	0.0	0.0	0.0	0.0	0.0		
36.0	4.5	1.4	2.3	1.5	1.1	1.7		
54.4	3.4	1.1	1.9	0.9	0.0	1.6		
83.0	36.5	14.6	28.8	21.1	14.5	28.0		
	mxPH 5.6 6.6 7.2 7.3 8.0 9.7 2 a1 0.0 16.8 30.3 36.0 54.4	mxPH mn0 5.6 5.7 6.6 9.2 7.2 10.8 7.3 10.1 8.0 11.3 9.7 12.6 2 2 a1 a2 0.0 0.0 16.8 0.0 30.3 0.0 36.0 4.5 54.4 3.4	7 6 small medium 26 1 low medium 4 13 mxPH mn02 Cl 5.6 5.7 0.2 6.6 9.2 4.5 7.2 10.8 9.0 7.3 10.1 19.3 8.0 11.3 25.2 9.7 12.6 71.0 2 2 16 a1 a2 a3 0.0 0.0 0.0 16.8 0.0 0.0 30.3 0.0 0.0 30.3 0.0 0.0 36.0 4.5 1.4 54.4 3.4 1.1	7 6 8 small medium large 26 1 7 low medium high 4 13 17 mxPH mn02 Cl N03 5.6 5.7 0.2 0.2 6.6 9.2 4.5 0.8 7.2 10.8 9.0 1.4 7.3 10.1 19.3 2.1 8.0 11.3 25.2 2.5 9.7 12.6 71.0 11.0 2 2 16 2 a1 a2 a3 a4 0.0 0.0 0.0 11.0 2 2 16 2 a1 a2 a3 a4 0.0 0.0 0.0 0.0 16.8 0.0 0.0 0.0 30.3 0.0 0.0 0.0 36.0 4.5 1.4 2.3 54.4 3.4 1.1 1.9	small medium large 26 1 7 low medium high 4 13 17 mxPH mn02 Cl N03 NH4 5.6 5.7 0.2 0.2 5.0 6.6 9.2 4.5 0.8 10.0 7.2 10.8 9.0 1.4 11.8 7.3 10.1 19.3 2.1 62.0 8.0 11.3 25.2 2.5 46.3 9.7 12.6 71.0 11.0 500.0 2 2 16 2 2 a1 a2 a3 a4 a5 0.0 0.0 0.0 0.0 0.0 16.8 0.0 0.0 0.0 0.0 30.3 0.0 0.0 0.0 0.0 36.0 4.5 1.4 2.3 1.5 54.4 3.4 1.1 1.9 0.9	small medium large 26 1 7 low medium high 4 13 17 mxPH mn02 Cl N03 NH4 oP04 5.6 5.7 0.2 0.2 5.0 1.0 6.6 9.2 4.5 0.8 10.0 1.0 7.2 10.8 9.0 1.4 11.8 3.6 7.3 10.1 19.3 2.1 62.0 25.6 8.0 11.3 25.2 2.5 46.3 20.2 9.7 12.6 71.0 11.0 500.0 295.6 2 2 16 2 2 2 a1 a2 a3 a4 a5 a6 0.0 0.0 0.0 0.0 0.0 0.0 16.8 0.0 0.0 0.0 0.0 0.0 30.3 0.0 0.0 0.0 0.0 0.0 36.0 4.5 1.4 2.3 1.5 1.1 54.4 3.4 1.1 1.9 0.9 0.0	small medium large 26 1 7 low medium high 4 13 17 mxPH mn02 Cl N03 NH4 oP04 P04 5.6 5.7 0.2 0.2 5.0 1.0 1.0 6.6 9.2 4.5 0.8 10.0 1.0 6.0 7.2 10.8 9.0 1.4 11.8 3.6 10.8 7.3 10.1 19.3 2.1 62.0 25.6 34.5 8.0 11.3 25.2 2.5 46.3 20.2 19.2 9.7 12.6 71.0 11.0 500.0 295.6 380.0 2 2 16 2 2 2 7 2 a1 a2 a3 a4 a5 a6 a7 0.0 0.0 0.0 0.0 0.0 0.0 0.0 16.8 0.0 0.0 0.0 0.0 0.0 0.0 30.3 0.0 0.0 0.0 0.0 0.0 0.0 36.0 4.5 1.4 2.3 1.5 1.1 1.7 54.4 3.4 1.1 1.9 0.9 0.0 1.6	small medium large 26 1 7 low medium high 4 13 17 mxPH mn02 Cl N03 NH4 oP04 P04 Chla 5.6 5.7 0.2 0.2 5.0 1.0 1.0 0.3 6.6 9.2 4.5 0.8 10.0 1.0 6.0 1.7 7.2 10.8 9.0 1.4 11.8 3.6 10.8 4.0 7.3 10.1 19.3 2.1 62.0 25.6 34.5 13.9 8.0 11.3 25.2 2.5 46.3 20.2 19.2 12.2 9.7 12.6 71.0 11.0 500.0 295.6 380.0 68.0 2 2 16 2 2 2 7 23 a1 a2 a3 a4 a5 a6 a7 0.0 0.0 0.0 0.0 0.0 0.0 16.8 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 30.3 0.0 0.0

34: By which we mean that low-speed rivers do not seem to have a systematic missing value problem.

35: In a real-life setting, we should *definitely* verify that this assumption is valid.

Right off the bat, missing cases seem to be over-represented in small rivers and under-represented in low-speed rivers. But upon further investigation (that is, comparing with the original dataset), we suspect that the under-representation of low-speed rivers is not problematic as it falls in-line with the numbers in the larger dataset.³⁴

Let us assume for now (in the interest of efficiency) that the fact that small rivers have a lot of missing cases (mostly Cl and Chla) is also not a problem.³⁵ The bulk of the missing values seem to come from either Cl, Chla, or P04. There is also a consistent 2 missing values across the board, but we cannot use the summary output to determine if they arise from the same two observations.

Which observations have missing NH4 values, say?

```
        season
        size
        speed
        mxPH
        mnO2
        CI
        NO3
        NH4
        oPO4
        Chla
        a1
        a2
        a3
        a4
        a5
        a6
        NA
        NA
        PO4
        Chla
        a1
        a2
        a3
        a4
        a5
        a6
        NA
        NA
        NA
        A1
        NA
        a1
        a2
        a3
        a4
        a5
        a5
```

While these observations also have missing values in other fields, they do have some non-missing fields as well. But they are both missing 6 of the predictor variables. How useful could they be in training a predictive model?³⁶ We can easily write a function that will compute how many missing cases there are for each observations.

```
Var1 Freq
0 306
1 20
2 12
6 2
```

Most observations have no missing cases, which is great news. There are a few with 1 or 2, but observations 62 and 199 are **wild cards**, with 6 missing predictors (out of 11). Based on the small number of such wild cards, we elect to remove them from the analysis.

IMPORTANT NOTES

• If we decide to remove observations for any reason whatsoever, we need to document the process that lead us to eliminate them, and make that process available to other analysts or to the audience.

36: The answer to that question depends on the model, of course.

■ Why do we remove the observations with 6 missing cases, but not the ones with 2 missing cases? Had there been observations with 4 missing cases, what should we have done? What factors could influence this decision?

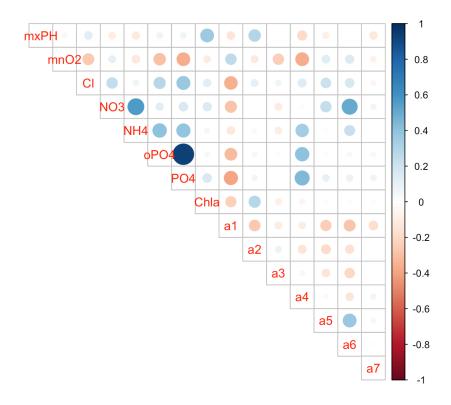
This dataset still contains observations with missing cases, however.

[1] 338

What can we do with the other observations for which values are missing?

One possibility is to use the set of complete observations to compute a **correlation matrix**, and to see if any numerical field is strongly correlated with another field. That way, if there is a missing value in the first field, the second could be used to impute it.

IMPORTANT NOTE: this approach only works for variables that are linearly correlated to a single other variable. Non-linear correlations and multi-variate associations will not be uncovered.



The correlation between P04 (which has missing cases) and oP04 (which does not, anymore) is clear. What is the nature of the relation? We use the set of complete cases to find it.

[1] 306

```
P04.oP04.model = lm(P04 ~ oP04, data=algae_blooms.nona)
P04.oP04.model
```

Coefficients:

```
(Intercept) oP04
51.811 1.203
```

The regression function is P04=51.811+1.2030P04 (we are not particularly interested in the fit statistics at this point).

```
Intercept = P04.oP04.model$coefficients[[1]]
Slope = P04.oP04.model$coefficients[[2]]
```

What are the observations for which P04 is missing?

```
which(is.na(algae_blooms.sna$PO4)==TRUE)
```

```
[1] 28 221 291 326 331 335
```

We can use the regression function to impute the missing P04 values.

We can clearly see that no values of P04 are missing anymore.

```
which(is.na(algae_blooms.sna2$P04)==TRUE)
```

```
integer(0)
```

That takes care of the missing values with strong linear correlation to another field. Where do we stand now?

```
summary(algae_blooms.sna2)
```

We suppress the output in the interest of legibility, but there are still some missing values. And we have exhausted the correlation trick. What else can we do?

There are many ways to tackle the problem, but we will use kNN imputation.³⁷ The principle is simple:

- 1. using some similarity/distance metric (typically based on the Euclidean distance between points), identify the k nearest (complete) neighbours of each observation with a missing case;
- 2. compute the mean value of the missing case in the k-group of complete observations, and use *that* value as the imputed value.

IMPORTANT NOTES

- As we have seen when we were discussing, we often suggest scaling the data when dealing with distance metrics. We elected not to scale the data explicitly here. How much of an effect can that have?
- We are going to be using DMwRs implementation of knnImputation() (below). How would you go about determining if the routine scales the data internally?

Sure enough, there are no further observations with incomplete cases.

```
table(apply(algae_blooms.sna2,1,
    function(x) sum(is.na(x))))
```

0 338

15.7.5 Principal Components

Principal components analysis (PCA) is typically used on the (numeric) predictor variables. There are methods that can be used to combine numeric and categorical variables, but for the purposes of this example, we will simply ignore the categorical fields.³⁸

38: We revisit this concept in Chapter 23.

in Chapter 21.

37: More details on this topic are available

pca.algae = algae_blooms.sna2[,4:11]
head(pca.algae)

Chla	PO4	oPO4	NH4	NO3	CI	mnO2	mxPH
50.0	170.000	105.000	578.000	6.238	60.800	9.8	8.00
1.3	558.750	428.750	370.000	1.288	57.750	8.0	8.35
15.6	187.057	125.667	346.667	5.330	40.020	11.4	8.10
1.4	138.700	61.182	98.182	2.302	77.364	4.8	8.07
10.5	97.580	58.222	233.700	10.416	55.350	9.0	8.06
28.4	56.667	18.250	430.000	9.248	65.750	13.1	8.25

We can scale the data frame using the scale() function in R:

head(scale(pca.algae))

mxPH	mnO2	CI	NO3	NH4	oPO4	PO4	Chla
-0.0019358	0.2748339	0.4423909	0.9488773	0.0611046	0.2795474	0.0145250	2.1362239
0.6101140	-0.5036258	0.3731037	-0.5578976	-0.0584991	3.1159254	1.4939011	-0.6253276
0.1729355	0.9667981	-0.0296707	0.6724831	-0.0719160	0.4606113	0.0794349	0.1855592
0.1204741	-1.8875541	0.8186771	-0.2492370	-0.2147992	-0.1043426	-0.1045862	-0.6196571
0.1029870	-0.0711482	0.3185826	2.2206563	-0.1368740	-0.1302752	-0.2610671	-0.1036382
0.4352426	1.7020100	0.5548406	1.8651183	-0.0239980	-0.4804704	-0.4167602	0.9113879

Notice the different values in the dataset. The principal components are obtained *via* the princomp() function.

```
pca.1 = princomp(scale(pca.algae))
summary(pca.1)
```

Importance of components:

```
Comp.1
                                    Comp.2
                                              Comp.3
                                                        Comp.4
Standard deviation
                       1.5334279 1.2022703 1.0900775 0.9329798
Proportion of Variance 0.2947973 0.1812179 0.1489744 0.1091293
Cumulative Proportion 0.2947973 0.4760152 0.6249896 0.7341189
                          Comp.5
                                    Comp.6
                                               Comp.7
                                                          Comp.8
Standard deviation
                       0.87500293 0.8081581 0.65499534 0.52248196
Proportion of Variance 0.09598775 0.0818822 0.05378649 0.03422468
Cumulative Proportion 0.83010663 0.9119888 0.96577532 1.000000000
```

If we can live with 75% of the variability in the numerical component of the predictors being explained by principal components, than we can reduce the dataset dimension by 4.

```
reduced.algae = data.frame(algae_blooms.sna2[,1:3],
    pca.1$scores[,1:4], algae_blooms.sna2[12:17])
head(reduced.algae)
```

```
season size speed
                      Comp.1
                                 Comp.2
                                            Comp.3
                                                                a1
                                                        Comp. 4
                                                                 0.0
                                                                      0.0
1 winter small medium 1.0634865
                                0.2877982
                                          1.6268674
                                                     0.26280655
2 spring small medium 2.1808329
                               0.5908937 -2.1258588
                                                     1.07795406
                                                                 1.4 7.6
3 autumn small medium 0.2097857 -0.4229638 0.6216107
                                                     0.52245855
                                                                 3.3 53.6
4 spring small medium 0.5213826
                               0.7948266 -1.0031723 -1.46518459
                                                                 3.1 41.0
5 autumn small medium 0.6477956 -0.8568203 1.1386691 -0.78026048 9.2 2.9
                high 0.1709107 -0.7049677 2.4338593 0.02250525 15.1 14.6
6 winter small
    a3 a4
            a5
                 a6
  0.0 0.0 34.2
                8.3
  4.8 1.9
          6.7
                0.0
3
  1.9 0.0
           0.0
                0.0
4 18.9 0.0 1.4
                0.0
 7.5 0.0 7.5 4.1
6 1.4 0.0 22.5 12.6
```

Whether this reduction proves useful or not will ultimately depend on what we would like to accomplish with the data; we will study this dataset again with a particular objective in mind in Section 20.6.

15.8 Exercises

- 1. The ability to monitor and perform early forecasts of various river algae blooms is crucial to control the ecological harm they can cause. The algae_blooms.csv dataset consists of: chemical properties of various water samples of European rivers; the quantity of seven (biological) algae in each of the samples, and other characteristics of the collection process for each sample.
 - a) Identify questions that could be tackled with this dataset.
 - b) Determine the structure of the dataset, and provide a summary of its features.
 - c) What can you say about the dataset, in terms of missing values and of the ranges of its values?
 - d) Do 2-way and 3-way tables (for the categorical variables) provide you with additional insights about the dataset?
 - e) Provide some simple (univariate and multivariate) visualizations of season, mn02, NH4+, a1, a3, and at least one other variable of your choice.
 - f) Does your analysis above suggest that there are anomalies in the dataset? Take action as needed.
 - g) Identify observations (cases) with only 1 missing value, 2 missing values, and so on. Are there strategies that would allow you to handle some of the cases (hint: what is the relationship between P04 and oP04, for instance)? Are there observations that should be removed from the dataset?
 - h) Produce a clean dataset to be used in analysis, with justification.

2. Consider the datasets

- GlobalCitiesPBI.csv 🗗
- 2016collisionsfinal.csv 🗗
- polls_us_election_2016.csv 🗅
- $HR_2016_Census_simple.xlsx \mathbb{Z}, and$

■ UniversalBank.csv 🗗.

For each dataset:

- a) Create a "data dictionary" to explain the different fields and variables. Can you find a source for these datasets online?
- b) Develop a list of questions you would like answered about the datasets.
- c) Investigate individual variables (through simple charts, univariate statistics, etc.).
- d) Repeat the process with bivariate investigations (though simple charts, joint distributions, variable interactions, etc.).
- e) Do you trust the dataset, or not? Support your answer. If you do not trust the dataset, flag potential invalid entries, anomalous observations, missing values, or outliers. How should these entries be treated?
- f) Does any of your analysis suggest that some of the variables should be transformed? Do any of the questions you developed in step 2 support such transformations? If so, transform the data appropriately.
- 3. Repeat the last question with any dataset of your liking.
- 4. The remaining exercises use the Gapminder Tools \square (there is also an offline version \square).
 - a) Explore the dataset with the Gapminder Tools in its default configuration. Do you think that there could be problems with the reported values? For instance, select Sweden and the United States from the checkbox menu on the right and follow their path from 1799 to 2018/2020. From what point onwards are the values sensible? What do you think is happening at the start of the time series?
 - b) Follow Eritrea for the same duration. Look up the country's independence date from Ethiopia. What do you think the measurements prior to that date represent?
 - c) Follow Austria for the same duration. Look up the historical timeline of the country's boundaries (Austria-Hungary, Anschluss, modern borders, etc.). What does that imply for the measurements?
 - d) Follow Finland for the same duration. What happens in 1809? Does that tell you anything about the way data is coded in the dataset?
 - e) De-select all countries and let the simulation run from 1799 to 2018/2020. Can you identify instances where a large subset of observations behaves in unexpected manners? If so, do you think that this is due to data cleaning/data processing issues?
 - f) Continue exploring the dataset. You may change which variables are displayed or work with some of the other visualization methods. Overall, do you think that the dataset is sound? Would you use it to run analyses? What are some of its strengths and weaknesses?